

My Thesis

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APPROVAL PAGE HERE

(OBTAIN AT THE GRADUATE SCHOOL)

MY THESIS

by

A. U. Thor

A THESIS

By Thesis Committee

_____, Chairperson

ABSTRACT

Thor, Alan Uthur, B.S., M.S., Mathematics, College of Arts and Sciences, North Dakota State University. November, 1998. My Thesis Major Professor: Dr. Merciless Ming.

Place abstract here.

DEDICATION

This work is dedicated to my mother and father and to the many others, though unnamed, who helped me in the completion of this task. (The Dedication is optional.)

ACKNOWLEDGMENTS

The acknowledgment is the place to thank the faculty, staff, family, and friends who have assisted you in preparing your thesis or dissertation. You may also acknowledge any financial support or special research materials given you.

Copyright permissions may also be acknowledged here by stating that: (1) permission has been granted for reproduction of tables, tests, and other copyright protected items and (2) gives the source of the permission.

Use a Preface rather than Acknowledgments when the research is discussed, for example, "the motivation for the study, the background of the project, the scope of the research, and the purpose of the paper" (Turabian, 1996, p. 7-8).

(Note: The Acknowledgments section is optional.)

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CHAPTER 1.

SAMPLE MATHEMATICS AND TEXT

1.1 In-line and Displayed Mathematics

The expression $\sum_{i=1}^{\infty} a_i$ is in-line mathematics, while the numbered equation

$$\sum_{i=1}^{\infty} a_i \tag{1.1}$$

is displayed and automatically numbered as equation 1.1.

Let H be a Hilbert space, C be a closed bounded convex subset of H , T a nonexpansive self map of C . Suppose that as $n \rightarrow \infty$, $a_{n,k} \rightarrow 0$ for each k , and $\gamma_n = \sum_{k=0}^{\infty} (a_{n,k+1} - a_{n,k})^+ \rightarrow 0$. Then for each x in C , $A_n x = \sum_{k=0}^{\infty} a_{n,k} T^k x$ converges weakly to a fixed point of T .[?]

Two sets of L^AT_EX parameters govern mathematical displays.¹ The spacing above and below a display depends on whether the lines above or below are short or long, as shown in the following examples.

A short line above:

$$x^2 + y^2 = z^2$$

and a short line below.

A long line above may depend on your margins

$$\sin^2 \theta + \cos^2 \theta = 1$$

as will a long line below. This line is long enough to illustrate the spacing for mathematical displays, regardless of the margins.

¹L^AT_EX automatically selects the spacing depending on the surrounding line lengths.

1.2 Mathematics in Section Heads $\int_{\alpha}^{\beta} \ln t dt$

Mathematics can appear in section heads. Note that mathematics in section heads may cause difficulties in typesetting styles with running headers or table of contents entries.

1.3 Theorems, Lemmata, and Other Theorem-like Environments

A number of theorem-like environments is available. The following lemma is a well-known fact on differentiation of asymptotic expansions of analytic functions.

Lemma 1 *Let $f(z)$ be an analytic function in \mathbb{C}_+ . If $f(z)$ admits the representation*

$$f(z) = a_0 + \frac{a_1}{z} + o\left(\frac{1}{z}\right),$$

for $z \rightarrow \infty$ inside a cone $\Gamma_\varepsilon = \{z \in \mathbb{C}_+ : 0 < \varepsilon \leq \arg z \leq \pi - \varepsilon\}$ then

$$a_1 = -\lim_{z \rightarrow \infty, z \in \Gamma_\varepsilon} z^2 f'(z), \quad (1.2)$$

Proof. Change z for $1/z$. Then $\Gamma_\varepsilon \rightarrow \bar{\Gamma}_\varepsilon = \{z \in \mathbb{C}_- : \bar{z} \in \Gamma_\varepsilon\}$ and

$$f(1/z) = a_0 + a_1 z + o(z). \quad (1.3)$$

Fix $z \in \bar{\Gamma}_\varepsilon$, and let $C_r(z) = \{\lambda \in \mathbb{C}_- : |\lambda - z| = r\}$ be a circle with radius $r = |z| \sin \varepsilon / 2$. It follows from (1.3) that

$$\frac{1}{2\pi i} \int_{C_r(z)} \frac{f(\lambda) d\lambda}{(\lambda - z)^2} = \sum_{m=0}^1 a_m \frac{1}{2\pi i} \int_{C_r(z)} \frac{(\lambda - z_0)^m d\lambda}{(\lambda - z)^2} + R(z), \quad (1.4)$$

where for the remainder $R(z)$ we have

$$\begin{aligned} |R(z)| &\leq r^{-1} \max_{\lambda \in C_r(z)} o(|z|) = r^{-1} \max_{\lambda \in C_r(z)} |\lambda| \cdot O(|z| + r) \\ &= \frac{|z| + r}{r} \cdot O(|z| + r) = \frac{1 + \sin \varepsilon}{\sin \varepsilon} \cdot O(|z|). \end{aligned}$$

Therefore $R(z) \rightarrow 0$ as $z \rightarrow \infty$, $z \in \bar{\Gamma}_{\varepsilon/2}$, and hence by the Cauchy theorem (1.4)

implies

$$\frac{d}{dz} f(1/z) = a_1 + R(z) \rightarrow a_1, \text{ as } z \rightarrow \infty, z \in \bar{\Gamma}_{\varepsilon/2},$$

that implies (1.2) by substituting $1/z$ back for z . ■

CHAPTER 2.

FEATURES OF THIS SHELL

2.1 Section Headings

Use the Section tag for major sections, and the Subsection tag for subsections.

Subsection This is some harmless text under a subsection.

Subsubsection This is some harmless text under a subsubsection.

Subsubsubsection This is some harmless text under a subsubsubsection.

Subsubsubsubsection

This is some harmless text under a subsubsubsubsection.

2.2 Tags

You can apply the logical markup tag Emphasized.

You can apply the visual markup tags **Bold**, *Italics*, Roman, Sans Serif, *Slanted*, SMALL CAPS, and Typewriter.

You can apply the special, mathematics only, tags **fraktur**, **BLACKBOARD BOLD**, and *CALLIGRAPHIC*. Note that blackboard bold and calligraphic are correct only when applied to uppercase letters A through Z.

You can apply the size tags `tiny`, `scriptsize`, `footnotesize`, `small`, `normalsize`, `large`, Large, **LARGE**, huge and Huge.

Text Tags	Mathematics Tags	Size Tags
Bold	Fraktur	tiny
Italics	Blackboard Bold	scriptsize
Roman	Calligraphic	footnotesize
Sans Serif		small
Slanted		large
Small Caps		large
Typewriter		huge
		Huge

Table 2.1: Available tags

This is a Body Math paragraph. Each time you press the Enter key, Scientific WorkPlace switches to mathematics mode. This is convenient for carrying out “scratchpad” computations.

Following is a group of paragraphs marked as Body Quote. This environment is appropriate for a short quotation or a sequence of short quotations.

The only thing we have to fear is fear itself. Franklin D. Roosevelt, Mar. 4, 1933

Ask not what your country can do for you; ask what you can do for your country. John F. Kennedy, Jan. 20, 1961

There is nothing wrong with America that cannot be cured by what is right with America. William J. “Bill” Clinton, Jan. 21, 1993

2.3 List Environments

You can create numbered, bulleted, and description lists using the tag popup at the bottom left of the screen.

1. List item 1
2. List item 2

(a) A list item under a list item.

The typeset style for this level is different than the screen style. The screen shows a lower case alphabetic character followed by a period while the typeset style uses a lower case alphabetic character surrounded by parentheses.

(b) Just another list item under a list item.

i. Third level list item under a list item.

A. Fourth and final level of list items allowed.

- Bullet item 1
- Bullet item 2

– Second level bullet item.

* Third level bullet item.

· Fourth (and final) level bullet item.

Description List Each description list item has a term followed by the description of that term. Double click the term box to enter the term, or to change it.

Bunyip Mythical beast of Australian Aboriginal legends.

APPENDIX A.

THE FIRST APPENDIX

The appendix fragment is used only once. Subsequent appendices can be created using the Chapter Section/Body Tag.

Following is a short bibliography. It has no relationship to the previous text, but can be used to show sample citations such as⁴ and.⁶ This typesetting style places each citation in a superscript position. If you want multiple citations to appear next to each other, either separate the citations using a superscripted comma like^{2,3,4} or type all of the citation keys inside a single citation, separating each with a comma like.^{2, 3, 4}

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